

**Indian National Physics Olympiad (INPhO)-2026**  
**HOMI BHABHA CENTRE FOR SCIENCE EDUCATION**  
**Tata Institute of Fundamental Research**  
**V. N. Purav Marg, Mankhurd, Mumbai, 400 088**

**Question Paper**

Date: 01 February 2026

Time: **09:00-12:00 (3 hours)**

Maximum Marks: **75**

**Instructions**

**Roll Number:**  -  -

1. This booklet consists of 10 pages and total of 6 questions. Write roll number at the top wherever asked.
2. Booklet to write the answers is provided separately. Instructions to write the answers are on the Answer Booklet.
3. Non-programmable scientific calculators are allowed. Mobile phones **cannot** be used as calculators.
4. Take as many data points as possible for the analysis.
5. **Please submit the Answer Sheet at the end of the examination.** You may retain the Question Paper.
6. Except for writing your roll number, no rough work or scribbling is allowed on the question paper.

**Table of Constants**

|                              |         |   |
|------------------------------|---------|---|
| Speed of light in vacuum     | $c$     | $3.00 \times 10^8 \text{ m}\cdot\text{s}^{-1}$                          |
| Magnitude of electron charge | $e$     | $1.60 \times 10^{-19} \text{ C}$  |
| Avogadro's number            | $N_A$   | $6.022 \times 10^{23} \text{ mol}^{-1}$                                 |
| Acceleration due to gravity  | $g$     | $9.81 \text{ m}\cdot\text{s}^{-2}$                                      |
| Universal Gas Constant       | $R$     | $8.31 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$                  |
|                              | $R$     | $0.0821 \text{ l}\cdot\text{atm}\cdot\text{mol}^{-1}\cdot\text{K}^{-1}$ |
| Boltzmann constant           | $k_B$   | $1.3806 \times 10^{-23} \text{ J}\cdot\text{K}^{-1}$                    |
| Permeability constant        | $\mu_0$ | $4\pi \times 10^{-7} \text{ H}\cdot\text{m}^{-1}$                       |
| One Atmospheric pressure     | atm     | $1.013 \times 10^5 \text{ Pa}$  |

| Question Number | <b>1</b> | <b>2</b> | <b>3</b> | <b>4</b> | <b>5</b> | <b>6</b> | <b>Total</b> |
|-----------------|----------|----------|----------|----------|----------|----------|--------------|
| Maximum Marks   | 12       | 12       | 11       | 10       | 18       | 12       | <b>75</b>    |

## 1. [12 marks] Find the flaw

Consider a non-conducting, charged, thin cubical shell with a uniform surface charge density. Consider the plane ABCD, which vertically and symmetrically divides the cubical shell (see figure). Six students independently solved for the electric field on the plane ABCD and presented six different answers, shown below in Figs. (a) to (f), each approximately depicting the electric field lines in the ABCD plane (the field line arrows are not shown). Consider each of the six answers, and for each, give

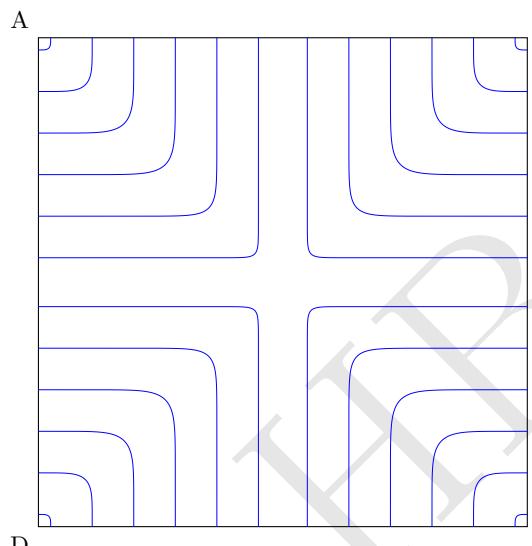
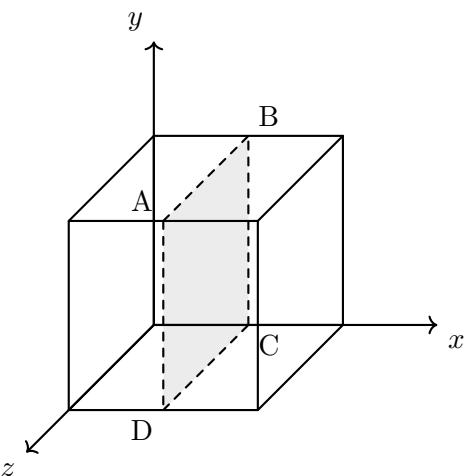
- at least one reason (based on a physics argument), explaining why it is incorrect

OR

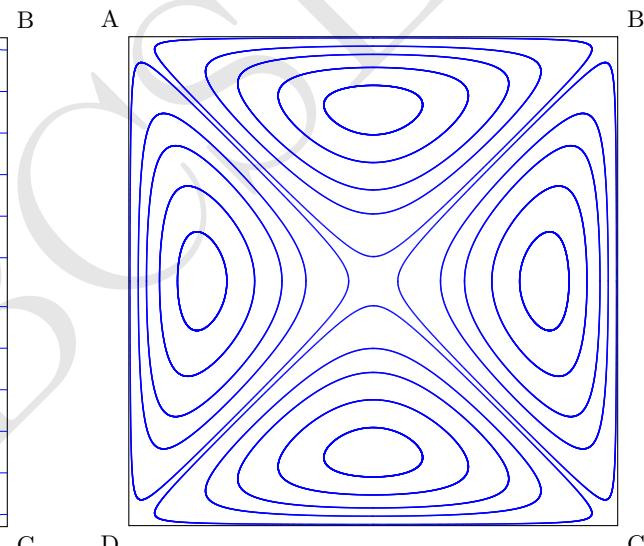
- at least two reasons why it **could** be correct.

Note that you are not required to obtain the correct depiction of the electric field or to provide a detailed derivation in this question.

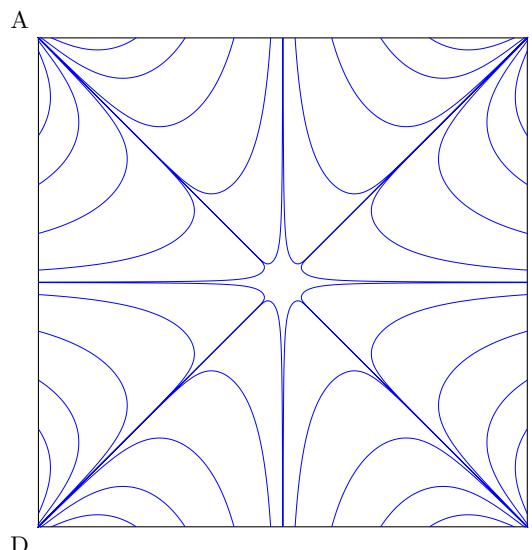
In none of the figures, adjacent field lines touch or intersect each other, although they may appear to do so in Fig. (c) and Fig. (e), where they are very close. In Fig. (d), the diagram indicates that no field is present. In Fig. (f),  $\otimes$  denotes a field directed along the  $-x$  axis, and  $\odot$  denotes a field directed along  $+x$  axis.



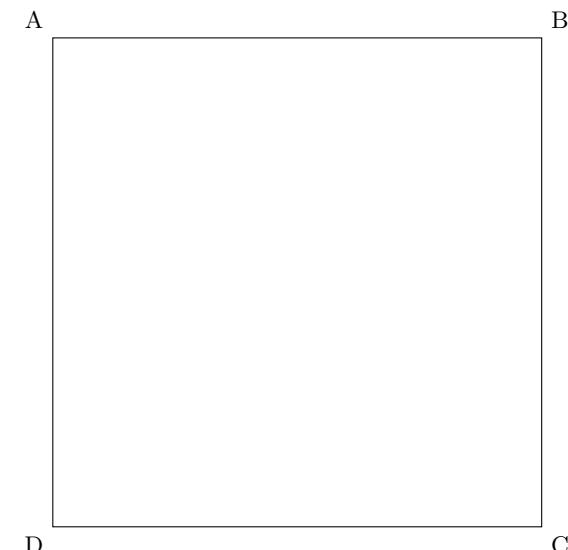
(a)



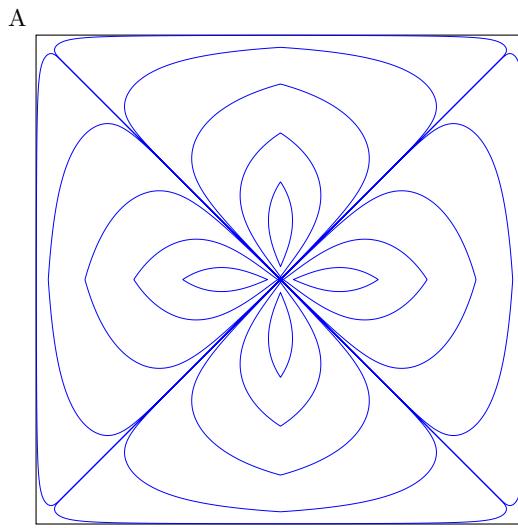
(b)



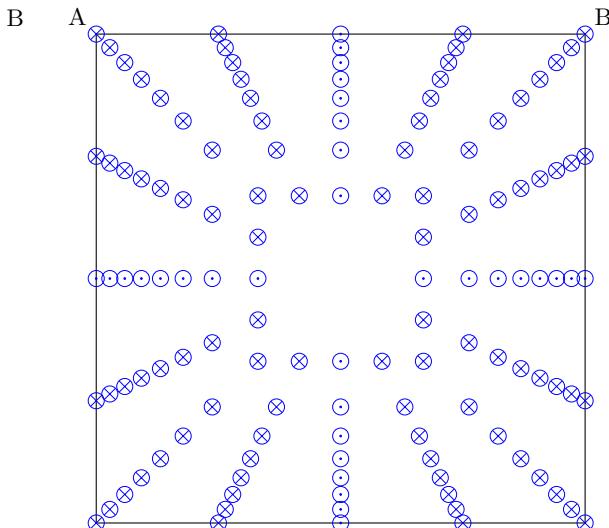
(c)



(d)



(e)



(f)

## 2. [12 marks] Current affairs

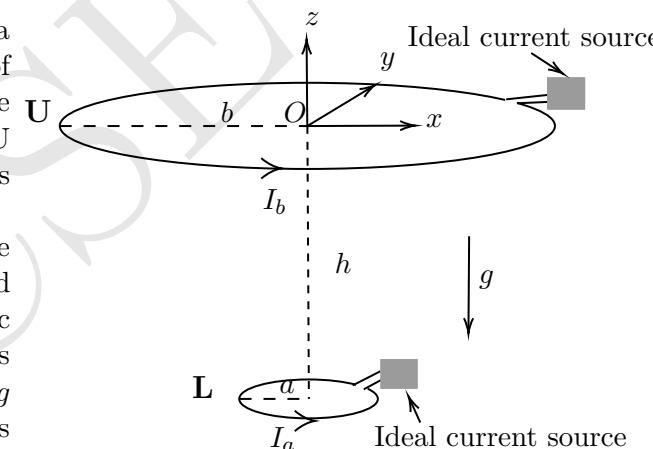
Consider two coaxial conducting circular loops: a lower loop L of radius  $a$  and an upper loop U of radius  $b$  (see figure). The planes of the loops are parallel and separated by a distance  $h$ . The loop U is held fixed in the  $x$ - $y$  plane, while the loop L is free to move vertically.

Each loop is connected to an ideal current source that maintains a constant current  $I_a$  in loop L and  $I_b$  in loop U. Assume  $a \ll b$ , so that the magnetic field produced by the loop U may be treated as uniform over the entire area of the loop L. Let  $g$  be the acceleration due to gravity. The system is initially in static equilibrium under gravity.

The loop L is then displaced very slowly by an external agent toward the loop U through a distance  $dh$ , while the currents in both loops are maintained constant by ideal power supplies.

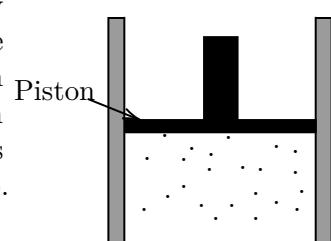
During this process, let the change in the gravitational potential energy of the loop L be  $dU_g$ , and the change in the energy stored in the magnetic field be  $dU_m$ . For the same process, let the extra work done by the power supplies connected to the lower and upper loops be  $dW_L$  and  $dW_U$ , respectively.

Express each of  $dU_g$ ,  $dU_m$ ,  $dW_U$ , and  $dW_L$  in terms of  $I_a$ ,  $I_b$ , the geometrical parameters  $(a, b, h, dh)$ , and any relevant constants, if they are non-zero.



## 3. Slow, smooth, and sudden

A vertical insulated cylinder fitted with a frictionless, movable, thermally conducting massless piston contains air at pressure  $p_0 = 1$  atm, volume  $V_i = 3.0$  L, and temperature  $T_0 = 300$  K. Assume the gas is ideal with a ratio of specific heats  $\gamma = 1.4$ . The system is initially in equilibrium with its surroundings at temperature  $T_0$  and pressure  $p_0$ . The piston is then moved so that the gas is compressed to a final volume  $V_f = 2.0$  L.



This compression is performed in three different ways:

(a) [3 marks] The piston is moved slowly, so that the compression remains quasistatic and

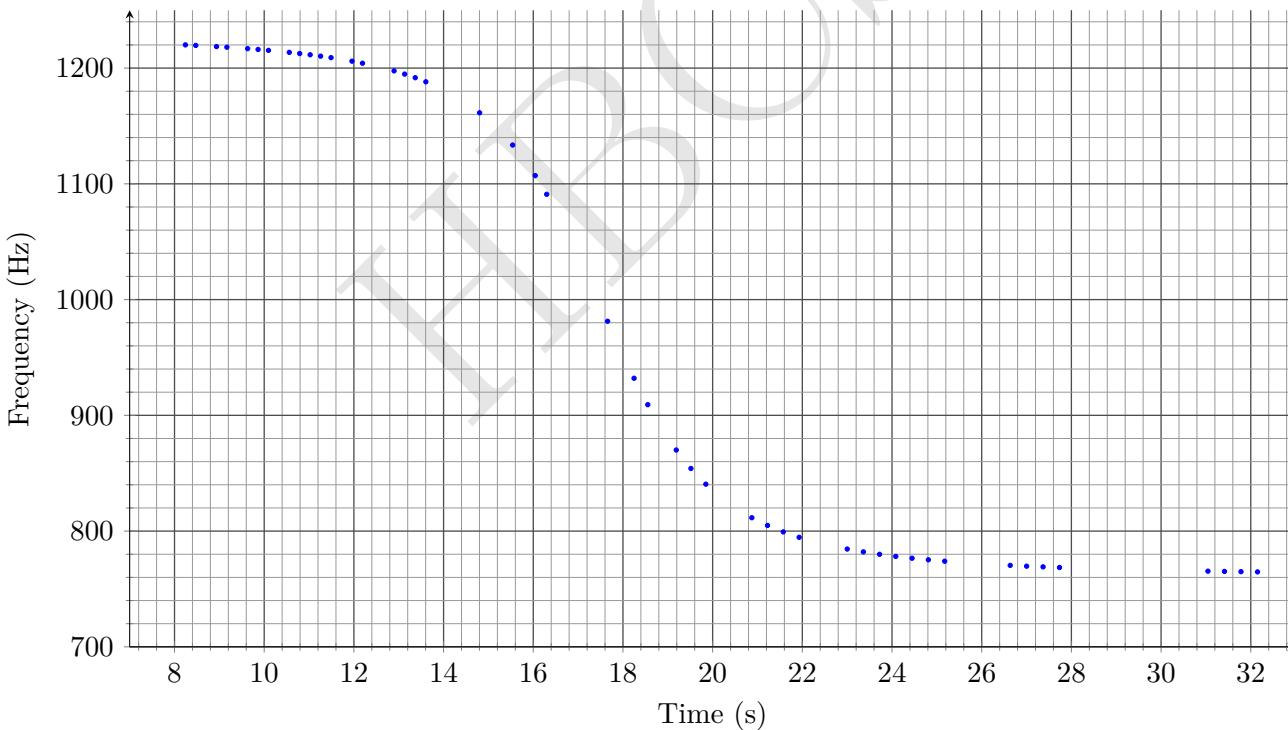
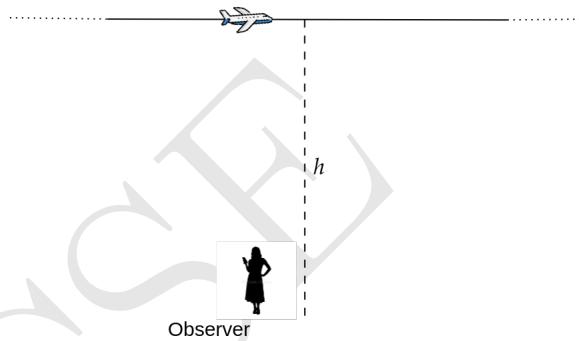
the gas stays in thermal equilibrium with the surroundings throughout (isothermal process). Calculate the total heat exchanged  $Q_a$  in the process.

(b) [3 marks] The piston is moved quickly but smoothly, so that during compression heat exchange with the surroundings is negligible (adiabatic and reversible). After compression, the gas is allowed to exchange heat with the surroundings without any change in volume, and it returns to the equilibrium temperature  $T_0$ . Calculate the total heat exchanged  $Q_b$  in the process.

(c) [5 marks] The piston is moved suddenly, producing a rapid, irreversible adiabatic compression. After compression, the gas reached a temperature  $T_c$ . The gas is now left to exchange heat with the surroundings without further change in the volume, and eventually returns to its equilibrium temperature  $T_0$ . Calculate  $T_c$  and the total heat exchanged  $Q_c$  in the process.

#### 4. A Curve You Can Hear

An aeroplane flies along a horizontal path, emitting sound at a constant frequency  $f_0$ . A stationary observer with a detector on the ground directly beneath the flight path records the sound frequency as the plane passes overhead, which is plotted below. The speed of sound in the medium is  $c_s = 340 \text{ m s}^{-1}$ .

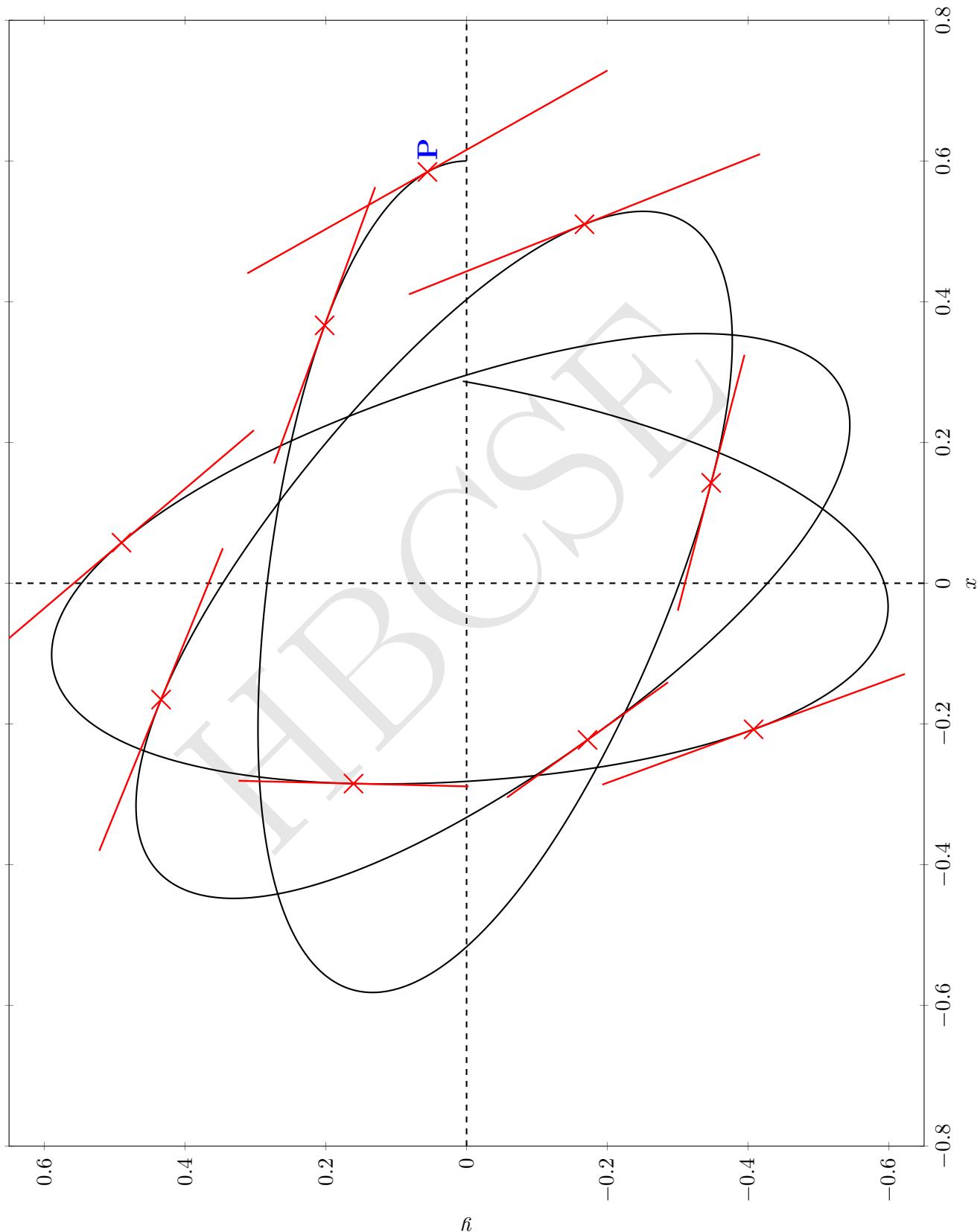


(a) [5 marks] Your task is to measure the speed of the aeroplane,  $v$ , from the graph. Express  $v$  in terms of quantities measurable from the graph, and define/mark these quantities on the graph reproduced in the Summary Answersheet. Calculate the value of  $v$ .

(b) [5 marks] Find the height  $h$  of the plane's flight path.

### 5. From Kepler's archive

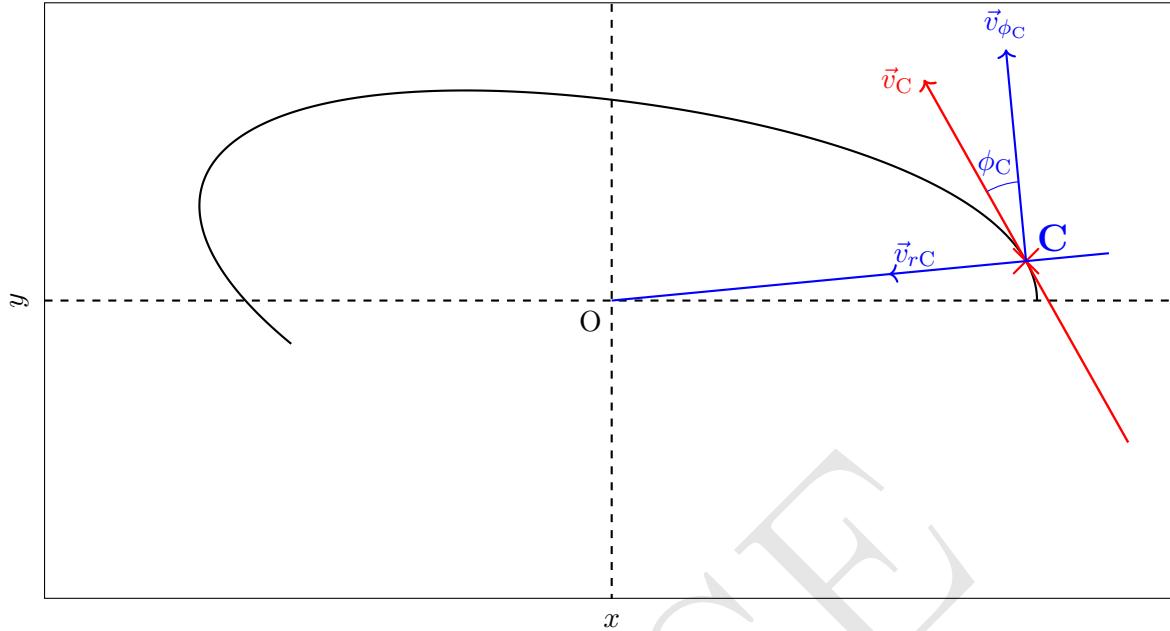
A short note found in Kepler's archive describes a curious central-force problem. The note states that the radial potential has the form  $U(r) = kr^n$ , where  $k > 0$  is a dimensional constant,  $n$  is a positive integer, and  $r$  is the distance from a fixed origin. Kepler also recorded the particle's precise trajectory by listing its  $x$ - $y$  coordinates in its plane of motion (see the figure below). His sketch includes several short tangent segments drawn at selected points, marked by  $\times$ .



The coordinates  $x$  and  $y$  are given in arbitrary units. Kepler's notes indicate that at point P, the kinetic energy is exactly one quarter of the total mechanical energy. He further noted that the

exponent  $n$  could be determined by performing calculations based on the graph and by constructing a linear plot. Unfortunately, the remainder of the manuscript explaining this method has been lost.

To understand what Kepler did, we define a few variables below. The figure below shows the trajectory of a particle moving under a central force.



Consider a fixed point C on the trajectory (shown by  $\times$ ), located at a distance  $r_C$  from the origin O. At point C, let the speed of the particle be  $v_C$ , and let the radial and tangential components of its velocity be  $v_{rC}$  and  $v_{\phi C}$ , respectively ( $\vec{v}_{\phi C}$  is  $\perp$  to  $\vec{v}_{rC}$ ).

The angle between  $\vec{v}_{\phi C}$  and the velocity vector  $\vec{v}_C$  is denoted by  $\phi_C$ .

At an arbitrary point on the trajectory, the particle is at a distance  $r$  from the origin, its speed is  $v$ , and the corresponding angle between  $\vec{v}$  and its tangential component  $\vec{v}_\phi$  is  $\phi$ .

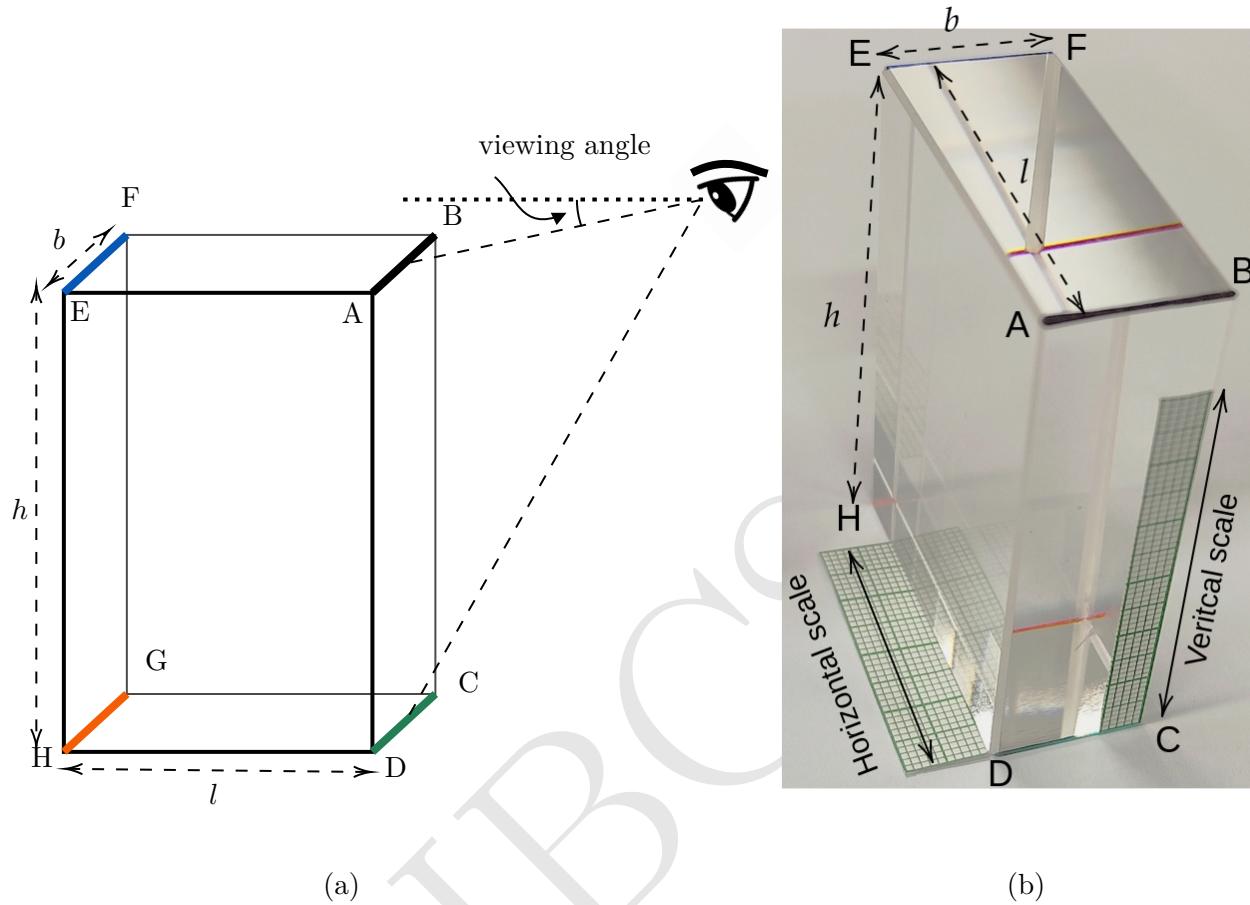
- [5 marks] The speed  $v$  at an arbitrary point can be written in terms of the speed at point C as  $v = \alpha v_C$ . Express  $\alpha$  in terms of  $r_C$ ,  $r$ ,  $\phi_C$ , and  $\phi$ .
- [13 marks] Two versions of Kepler's diagram are given in the answer sheet: one with tangents drawn and one without. You may use either or both figures as needed.

Use these to devise a method to find the value of  $n$ . Perform all relevant analyses using the figures provided on the answer sheet. Finally, use the graph paper at the end of the answer sheet for plotting a linear graph to determine  $n$ , and report any necessary data tables in the detailed answersheet.

HBCSE

### 6. Perspective matters

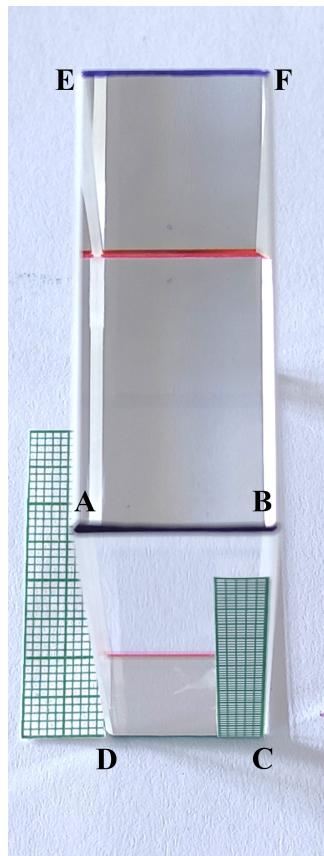
Consider a glass slab (ABCDHGFE) of dimensions  $(l \times b \times h)$ . The slab is placed on its base (CDHG), and viewed at different viewing angles with the vertical face (ABCD) facing the observer (see Fig. (a)). The edges of the glass slab are coloured as shown in Fig. (a). A piece of graph paper is placed next to the base (CDHG). Another piece of graph paper is pasted on the vertical face (ABCD) of the slab (see Fig. (b)). The least count of both the pasted graph papers is 1 mm.



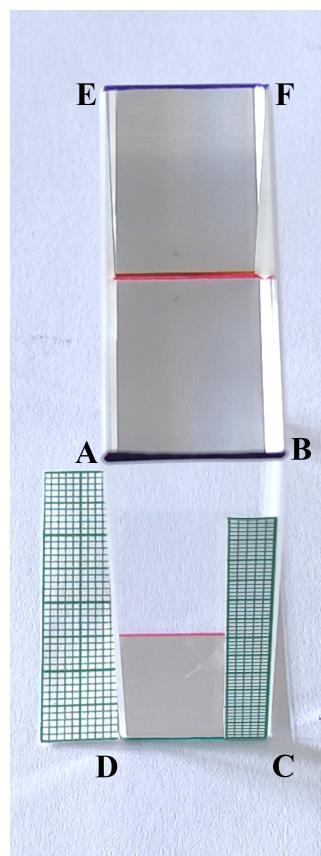
The task is to determine the refractive index  $\mu_g$  of the glass slab from a series of photographs of the slab taken from different viewing angles (by lowering the eye position) shown in Figs. (i) to (vi) on the next page. The viewing angle decreases progressively from Figs. (i) to (vi). Take the refractive index of air  $\mu_a$  to be 1.00. In this exercise, focus your attention on the red line visible through the vertical face (ABCD) only.

- [2 marks] Mark and state the measurable quantities in the photo given in the summary answer sheet, that can be used in subsequent parts for measuring the refractive index of the slab.
- [4 marks] Draw a ray diagram showing these measured quantities, and the relevant given dimensions of the slab. Derive an expression for the refractive index  $\mu_g$  of the glass slab in terms of the measured quantities that you have decided to use.
- [6 marks] Calculate the value of  $\mu_g$ , by plotting a linear graph. Report your datatable in the detailed answersheet.

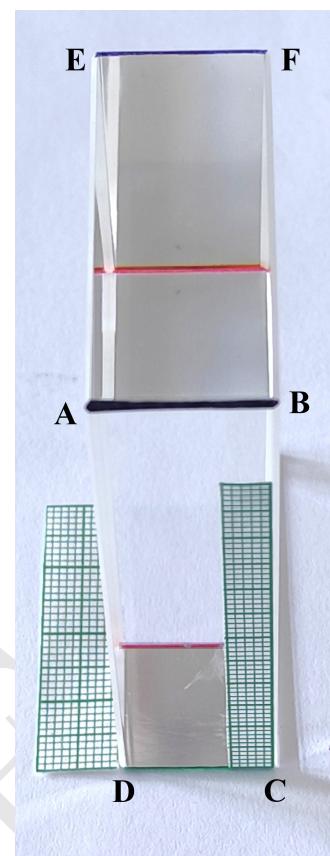
HBCSE



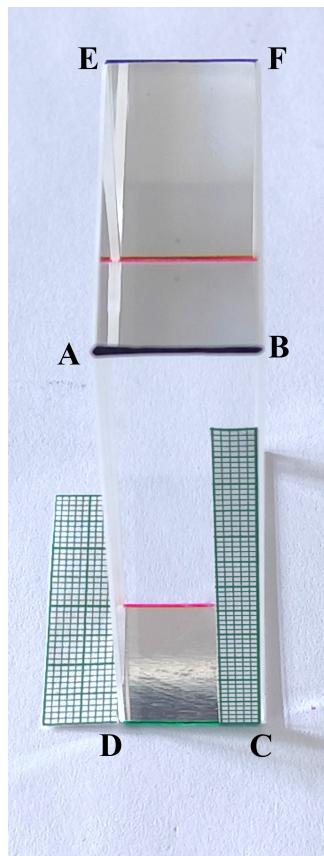
(i)



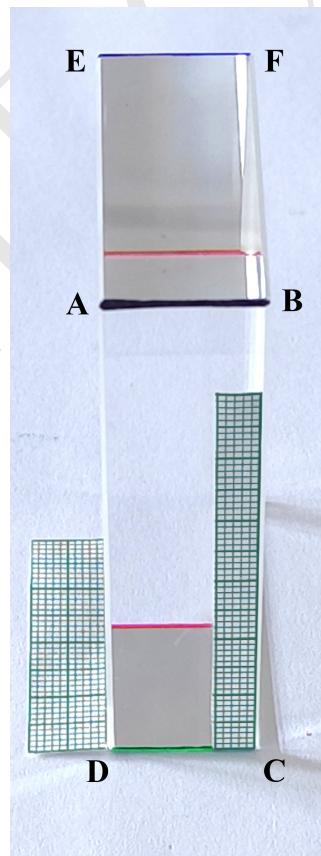
(ii)



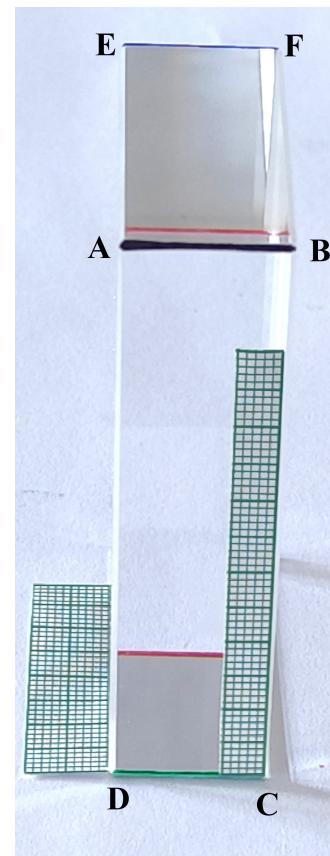
(iii)



(iv)



(v)



(vi)