Indian National Physics Olympiad - 2012 Solutions

Please note that alternate/equivalent solutions may exist. Brief solutions are given below.

1. (a)
$$\omega_{i+1} = \frac{7}{13}\omega_i + \frac{6}{13}\frac{v}{r}$$

(b)
$$\omega^* = \frac{v}{r}$$

Argument : Initially ω_i increases until it reaches a value $v = \omega^* r$, i.e. the speed of the falling ball. Thereafter the ball merely "touches" the sphere and does not impart it any momentum.



(f) At z_c atmospheric pressure should be equal to saturation pressure. Condition is

$$p_{0}\left(\frac{T_{0}-\Gamma z_{c}}{T_{0}}\right)^{\gamma/1-\gamma} = p_{s0} \exp\left[\frac{Lm_{v}}{R}\left(\frac{1}{T_{s0}}-\frac{1}{T_{0}-\Gamma z_{c}}\right)\right]$$
4. (a) Magnetic field =
$$\begin{cases} \frac{\mu_{0}NI}{l}\hat{k} & \rho < r\\ \rho > r & \\ \text{Value of magnetic field} = \begin{cases} 1.26 \times 10^{-2} \text{ T} & \rho < r\\ \rho > r & \\ \text{where } \rho \text{ is the radial distance.} & \\ (b) L = \frac{\mu_{0}N^{2}\pi r^{2}}{l} & \\ \text{Value of } L = 1.97 \times 10^{-2} \text{ H} & \\ (c) E = 3.95 \text{ J} & \\ (d) i = \frac{e}{R}(1-e^{-Rt/L}) + i_{0}e^{-Rt/L} & \text{if } i_{0} \neq 0 & \\ (e) e = iR + L\frac{di}{dt} - i\frac{Lv}{l+vt} & \\ \text{where } L = \mu_{0}N^{2}\pi r^{2}/(l+vt) & \\ (f) \text{ Electric field} = \begin{cases} \frac{\mu_{0}Ni_{0}\omega\rho}{2l}\sin(\omega t) & \rho < r \\ \frac{\mu_{0}Ni_{0}\omega r^{2}}{2\rho l}\sin(\omega t) & \rho > r \\ (g) \text{ The plot of } E \text{ with radial distance:} & \\ \end{cases}$$

radial distance

Lines of forces: Note, the lines of force are dense up to $\rho=r$ and increasingly sparse thereafter.

r



5. (a) Since $\hbar\omega_0 < E_b$, hence no ionisation by a single photon is possible.



(g)
$$F_0 = \frac{E^2 \pi \epsilon_0}{e^3}$$

(h) approx 174 V·m⁻¹ which is physically possible.