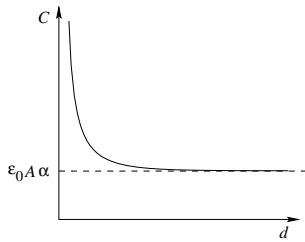


Indian National Physics Olympiad - 2013 Solutions

PLEASE NOTE THAT ALTERNATE/EQUIVALENT SOLUTIONS MAY EXIST. Brief solutions are given below.

1. (a) $C = \frac{\epsilon_0 A \alpha}{1 - e^{-\alpha d}}$

(b)



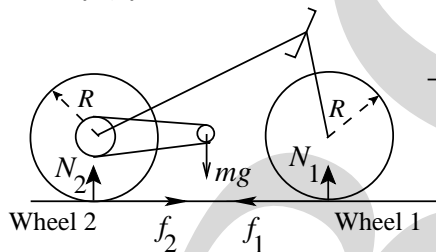
(c) Charge = $\frac{\epsilon_0 A \alpha V}{1 - e^{-\alpha d}}$

(d) $\vec{E}(x) = \frac{\alpha V e^{-\alpha x}}{1 - e^{-\alpha d}} \hat{x}$

2. (a) $\phi = \sin^{-1} \left(\frac{nh}{d\sqrt{2m_0K}} \right)$

(b) $d \approx 2.4 \text{ \AA}$

3. (a) Here f_1, f_2 are frictional forces and N_1, N_2 are normal reactions.



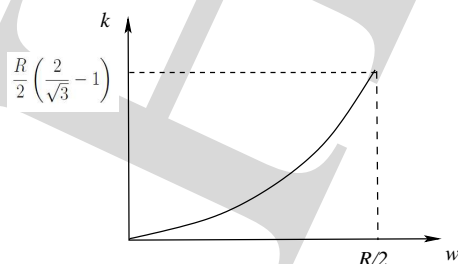
(b) $a = \frac{\tau}{MR^2 + 2I} R$

(c) $a \leq \frac{\mu g/2}{\left(1 - \frac{\mu}{4}\right)}$

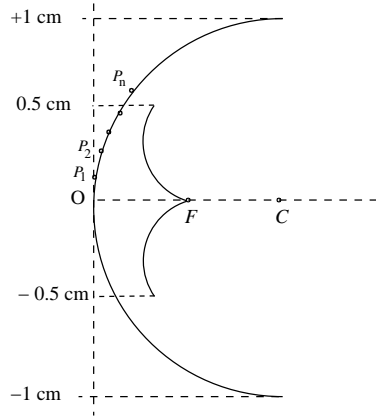
(d) $a_m = 2g/3$

4. (a) $k = \frac{R}{2} \left[\frac{R}{(R^2 - \omega^2)^{1/2}} - 1 \right]$

(b)



(c)



5. (a) Torque = $\frac{2\mu_0 I^2 (a^2 + b^2) abd \sin \phi}{\pi [(a^2 - b^2)^2 + 4a^2 b^2 \sin^2 \phi]} \hat{z}$

(b) $\phi = \alpha; -\alpha; \pi - \alpha; \pi + \alpha$
where $\alpha = \sin^{-1} [(a^2 - b^2)/2ab]$

6. (a) $g(r, \theta, \dot{r}, \dot{\theta}) = \frac{F(r)}{m} + r\dot{\theta}^2$

(b) From null azimuthal component

$$2\dot{r}\dot{\theta} + r\ddot{\theta} = 0$$

$$\frac{d}{dt}(r^2\dot{\theta}) = 0$$

$$\frac{d}{dt}(mr^2\dot{\theta}) = 0$$

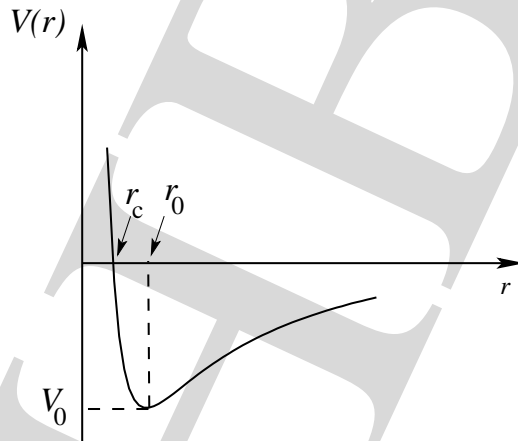
$$\frac{d}{dt}L = 0$$

$$\Rightarrow L = \text{constant}$$

(c) $E = \frac{m(\dot{r}^2 + r^2\dot{\theta}^2)}{2} - \frac{GMm}{r}$

(d) $V(r) = \frac{L^2}{2mr^2} - \frac{GMm}{r}$

(e)



where $r_0 = \frac{L^2}{GMm^2}$, $r_c = \frac{L^2}{2GMm^2}$ and $V_0 = -\frac{G^2 M^2 m^3}{2L^2}$

(f) For $E > 0$ orbit is hyperbola. For $E < 0$ orbit is ellipse. At $r = r_0$ orbit is circular.

(g) $r_0 = \frac{L^2}{GMm^2}$

$$(h) T_r = 2\pi\sqrt{\frac{r_0^3}{GM}}$$

$$(i) n > -3$$

$$7. (a) \Gamma_a = \frac{(1 - \gamma_a)m_a g}{\gamma_a R} \text{ or } -\frac{m_a g}{C_a}$$

where $\gamma_a = 7/5$ (ratio of specific heats at constant pressure and volume) and C_a is molar specific heat at constant pressure for air.

$$|\Gamma_a| \approx 0.01^\circ\text{K} \cdot \text{m}^{-1}$$

$$(b) \Gamma_b = -\frac{m_a g T_b}{C_b T_a}$$

$$(c) \ddot{z} = g \left(\frac{m_a T_b}{T_a m_b} - 1 \right)$$

$$(d) z_0 = \frac{T_0}{\Gamma_a} \left[1 - \left(\frac{m_b}{m_a} \right)^{1/(\eta-1)} \right]$$

where $\eta = C_a/C_b$.

$$(e) \text{Condition: } C_a > C_b$$

$$\omega = g \sqrt{\frac{m_a(\eta - 1)}{C_a T_0}} \left(\frac{m_a}{m_b} \right)^{1/(\eta-1)}$$

$$(f) \tau \approx 95 \text{ s}$$